



# Limitations of Newtonian-noise cancellation in underground detectors

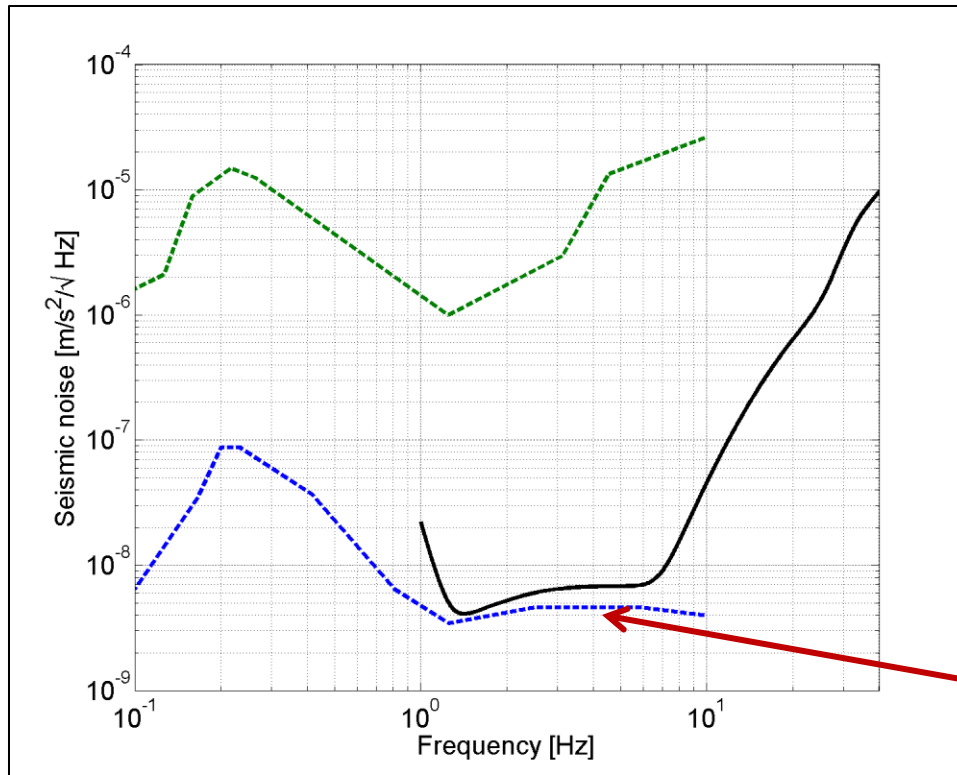
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# ET Requirement

ET-C sensitivity expressed as seismic-noise equivalent through gravitational coupling



Worst case assumption:  
All seismic displacement  
due to P-waves.

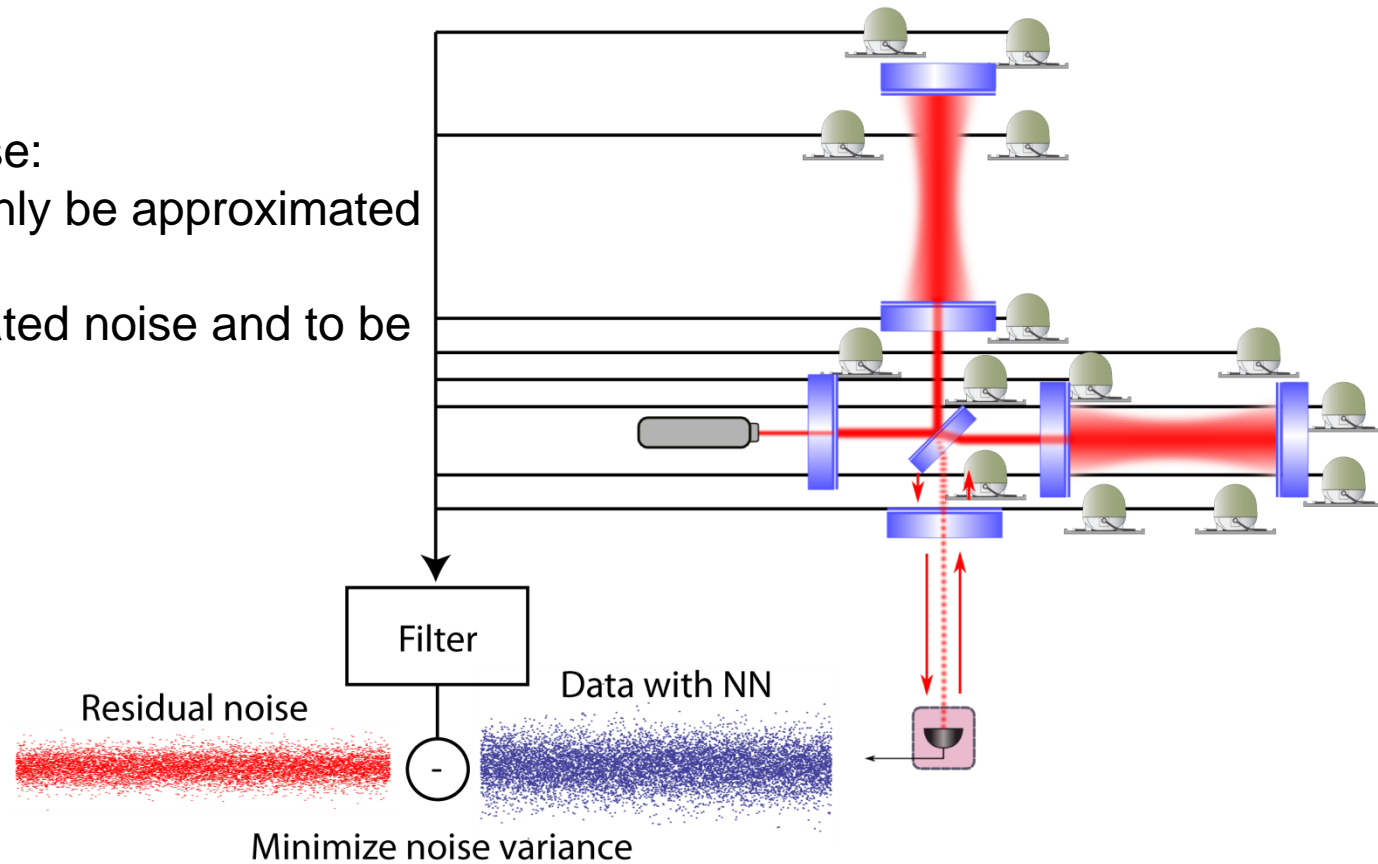
No site on Earth with  
average temperature above  
0°C has seismic noise below  
this line.



# Coherent Noise Cancellation

## Challenges:

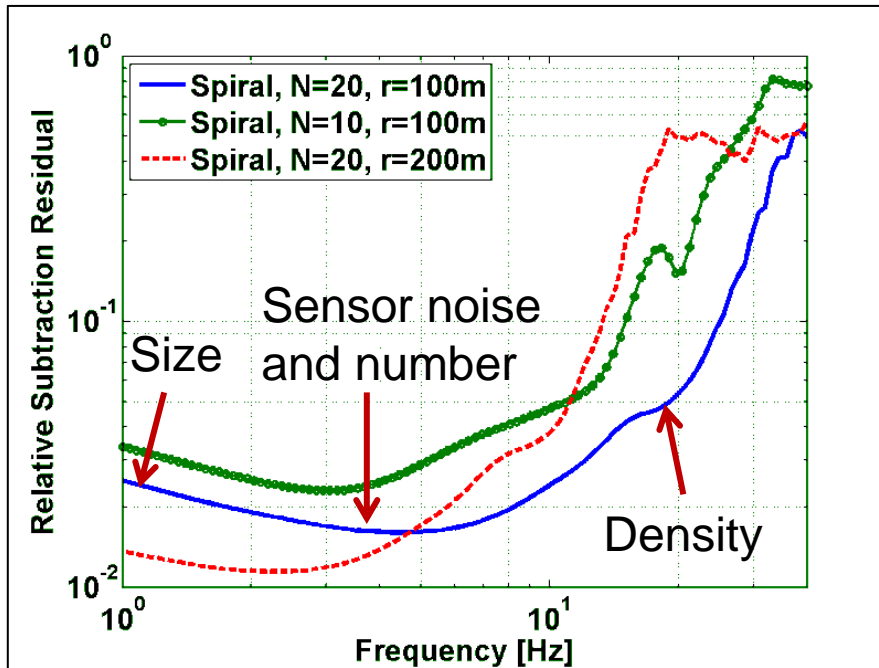
1. Non-stationary noise:  
Optimal filter can only be approximated
2. Correlated noise:  
Disentangle correlated noise and to be eliminated signal





# Previously

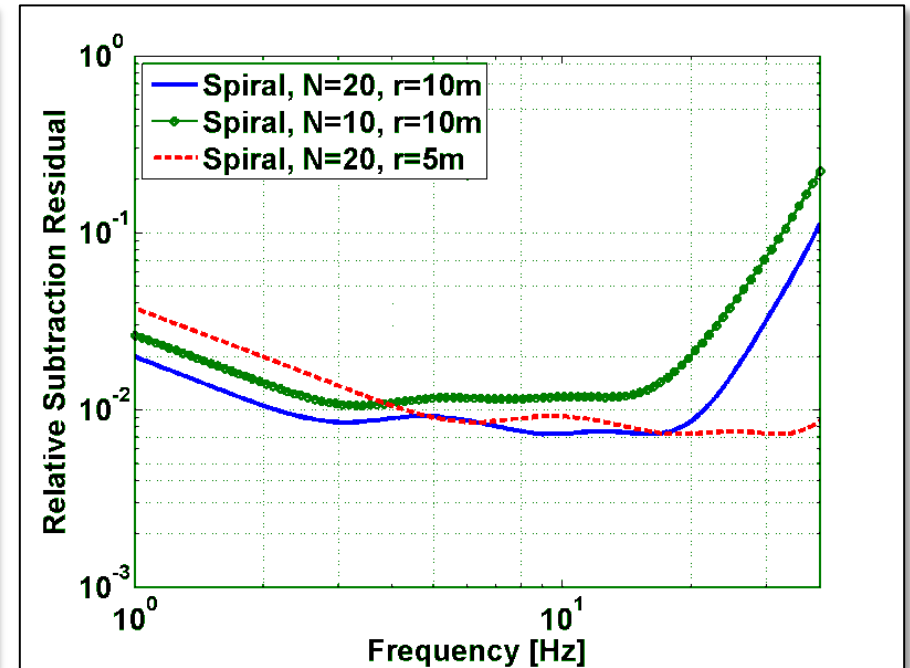
## Rayleigh-NN cancellation



Challenges:

- $\xi_z$  at TM uncorrelated with NN
- $\xi_{hor}$  has S-wave contribution

## Infrasound-NN cancellation



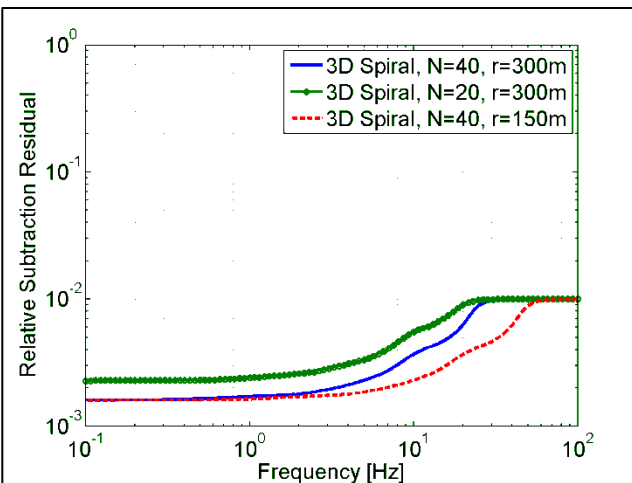
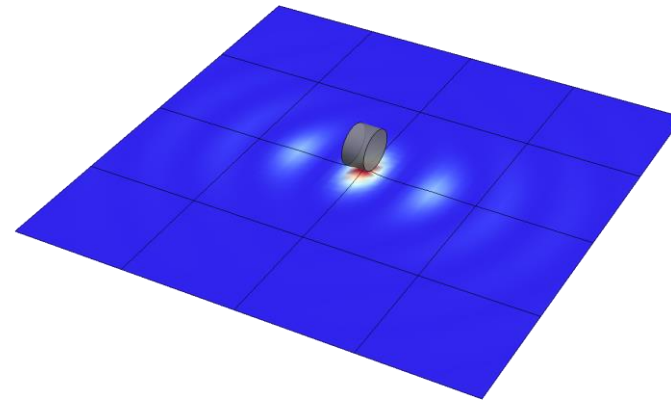
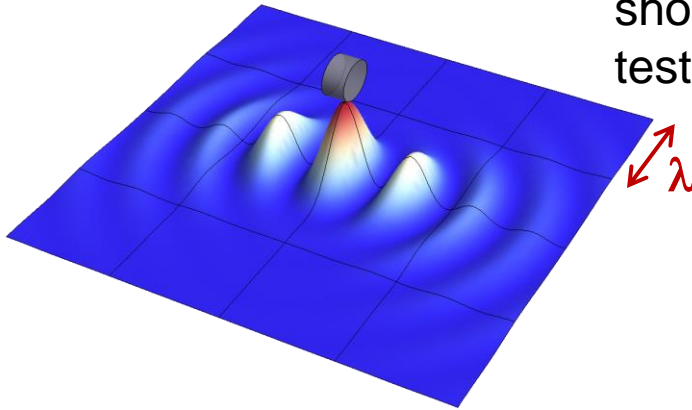
Challenges:

- Subtract NN from 3D field with 2D array
- No directional information from sensors



# P-Wave Subtraction

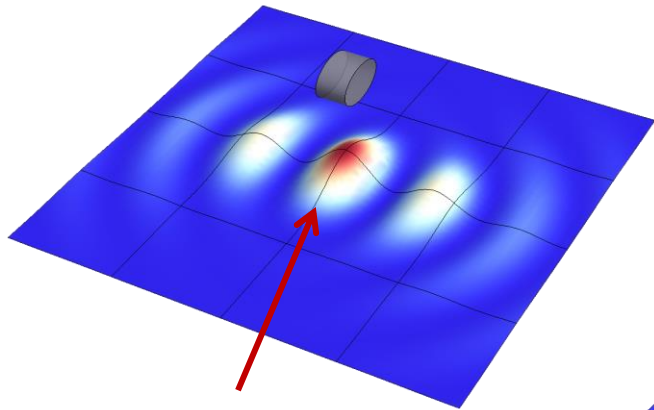
If there are only P-waves, all seismometers should be placed as close as possible to the test mass.



Subtraction residuals determined by number and SNR of seismometers.

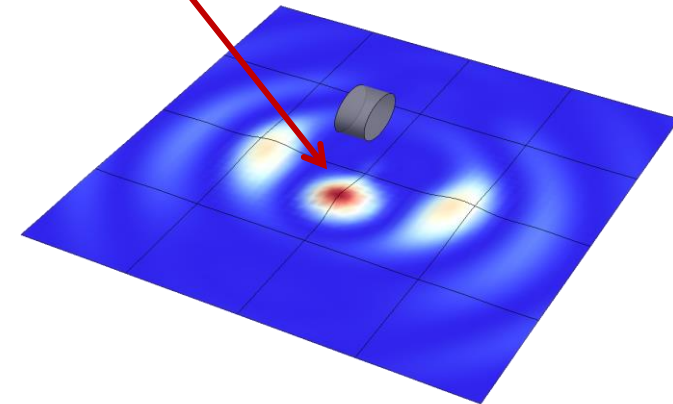
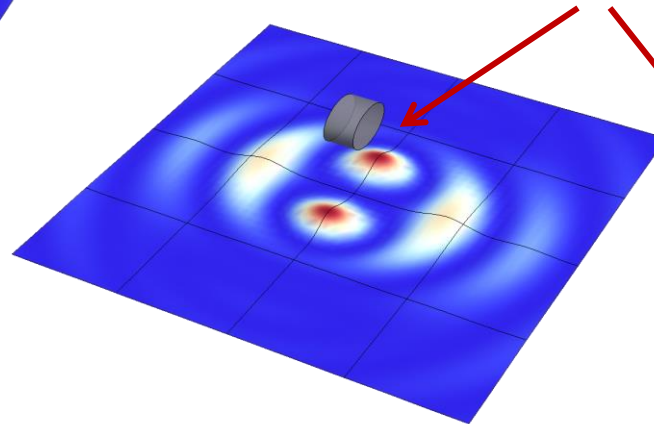


# Body-Wave Subtraction



If ET budget can only pay for one seismometer per test mass, place it here.

Second and third seismometer at right angle to distinguish between S and P waves (no correlation with NN).

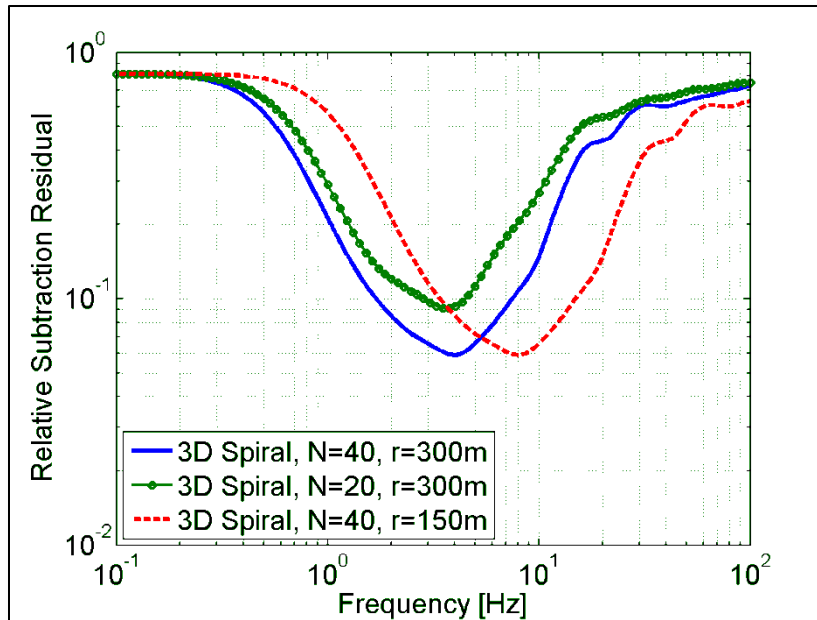


Mixing ratio:  $P/(S+P)=0.33$

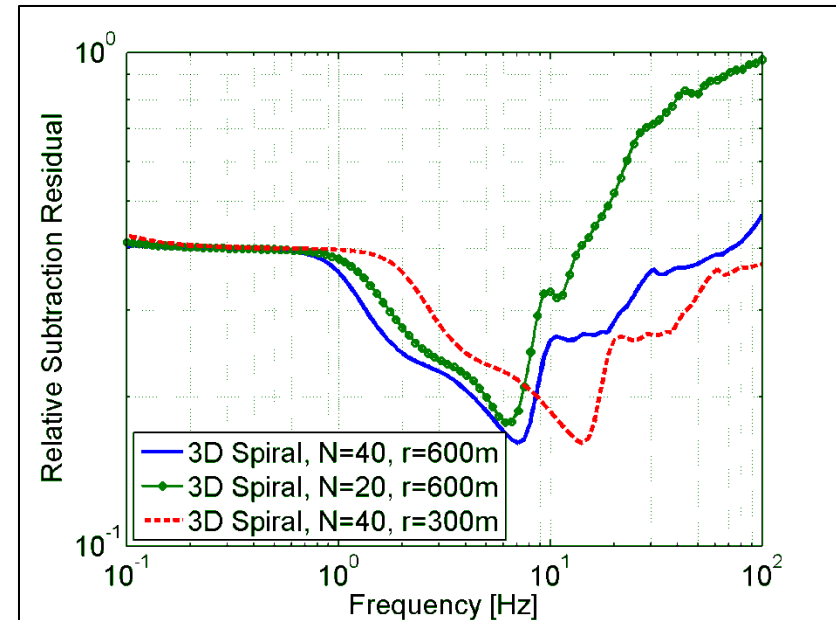


# Subtraction Residuals

Seismometers



Seismic strainmeters



1. All sensors oriented along arm
2. Mixing ratio:  $P/(S+P)=0.33$



# Possible Solutions

1. Calculate residuals using three-axis seismometers
2. Calculate residuals using seismic strainmeters in arbitrary orientations
3. Combine seismometers and strainmeters
4. Investigate optimal array configurations
5. Look at seismic data to estimate mixing ratio





# Limits in Array Size

Array needs to be big enough so that all significant density perturbations happen inside confines of the array.



How big is big enough?

**Example: grav acc from point force**

$$\delta \vec{a}(\vec{r}_0, t) = \frac{G}{r_0^3} (\vec{e}_f - 3(\vec{e}_f \cdot \vec{e}_{r_0})\vec{e}_{r_0}) \int_0^{r_0/\alpha} d\tau \tau F(t - \tau) + \frac{G}{r_0 \alpha^2} (\vec{e}_f \cdot \vec{e}_{r_0})\vec{e}_{r_0} F(t - r_0/\alpha)$$

Immediate perturbation

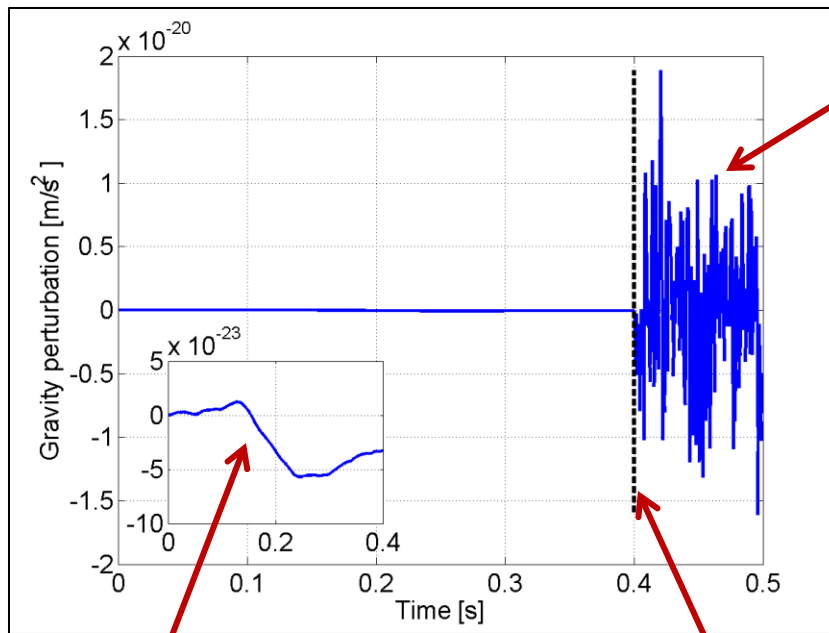
Distance between point force and test mass

Delayed perturbation



# Radiating Point Source

All seismic noise coming from one point source switched on at  $t=0$ :



Conventional NN from ambient seismic fields

While NN from approaching wavefronts cannot be subtracted, it is also very low frequency and likely unimportant.

NN from approaching wavefront

Arrival of wavefront at test mass